

CALCULATIONS USING SIGNIFICANT FIGURES

Name Key

When multiplying and dividing, limit and round to the least number of significant figures in any of the factors.

Example 1: $23.0 \text{ cm} \times 432 \text{ cm} \times 19 \text{ cm} = 188,784 \text{ cm}^3$
The answer is expressed as $190,000 \text{ cm}^3$ since 19 cm has only two significant figures.

When adding and subtracting, limit and round your answer to the least number of decimal places in any of the numbers that make up your answer.

Example 2: $123.25 \text{ mL} + 46.0 \text{ mL} + 86.257 \text{ mL} = 255.507 \text{ mL}$
The answer is expressed as 255.5 mL since 46.0 mL has only one decimal place.

Perform the following operations expressing the answer in the correct number of significant figures. Write units.

- $1.35 \text{ m} \times 2.467 \text{ m} = \underline{3.33 \text{ m}^2}$
- $1.035 \text{ m}^2 + 42 \text{ m} = \underline{25 \text{ m}}$
- $12.01 \text{ mL} + 35.2 \text{ mL} + 6 \text{ mL} = \underline{53 \text{ mL}}$
- $55.46 \text{ g} - 28.9 \text{ g} = \underline{26.6 \text{ g}}$
- $.021 \text{ cm} \times 3.2 \text{ cm} \times 100.1 \text{ cm} = \underline{6.7 \text{ cm}^3}$
- $0.15 \text{ cm} + 1.15 \text{ cm} + 2.051 \text{ cm} = \underline{3.35 \text{ cm}}$
- $150 \text{ L}^3 + 4 \text{ L} = \underline{37.5 \text{ L}^2} = \underline{40 \text{ L}^2}$
- $505 \text{ kg} - 450.25 \text{ kg} = \underline{55 \text{ kg}}$
- $1.252 \text{ mm} \times 0.115 \text{ mm} \times 0.012 \text{ mm} = \underline{1.7 \times 10^{-3} \text{ mm}^3} \text{ or } \underline{0.0017 \text{ mm}^3}$
- $1.278 \times 10^3 \text{ m}^2 + 1.4267 \times 10^2 \text{ m} = \underline{8.958 \text{ m}}$

Background:

- A mole is defined as 6.02×10^{23} particles (aka Avogadro's number). This is similar to a dozen being defined as 12 particles. In chemistry these "particles" are most often atoms, molecules, or ions.

$$1 \text{ mole} = 6.02 \times 10^{23} \text{ particles}$$

- Molar mass is the mass (usually in grams) of 1 mole of particles. The molar mass of a substance is determined by its chemical formula. We can find the molar mass of a substance by using the atomic masses on the periodic table.

Examples include: the molar mass of Na is 23.0 g/mol; the molar mass of Br₂ is (2 x 79.9 =) 159.8 g/mol; the molar mass of H₂O is (2 x 1.0 + 16.0 =) 18.0 g/mol.

$$1 \text{ mole} = (\text{Molar Mass from the Periodic Table}) \text{ grams}$$

Remember that in the process of dimensional analysis, we use equivalent statements to write ratios (fractions) that can be used to convert from one unit to another.

Example 1: What is the mass of 0.875 moles of CO₂?

$$0.875 \text{ moles CO}_2 \times \frac{44.0 \text{ grams}}{1 \text{ mole}} = 38.5 \text{ grams CO}_2$$

Example 2: How many atoms of Al are in a 255 gram sample of Al?

$$255 \text{ grams Al} \times \frac{1 \text{ mole Al}}{27.0 \text{ grams Al}} \times \frac{6.02 \times 10^{23} \text{ atoms Al}}{1 \text{ mole Al}} = 5.69 \times 10^{24} \text{ atoms Al}$$

Try These: Show your work for each problem using dimensional analysis. Put units on every number that you write down (in your work AND on your answer).

- What is the mass of 5.07×10^{22} ^{atoms} ~~molecules~~ of C?

$$5.07 \times 10^{22} \text{ atoms} \times \frac{1 \text{ mol}}{6.02 \times 10^{23} \text{ atoms}} \times \frac{12.0 \text{ g}}{1 \text{ mol}} = 1.01 \text{ g C}$$

- How many ~~molecules~~ ^{atoms} of S ~~would be~~ in 4.75 moles of S?

$$4.75 \text{ mol S} \times \frac{6.02 \times 10^{23} \text{ atoms}}{1 \text{ mol S}} = 2.86 \times 10^{24} \text{ atoms}$$

- How many atoms of gold are in a 1.00 kg gold bar?

$$1.00 \text{ kg Au} \times \frac{1000 \text{ g}}{1 \text{ kg}} \times \frac{1 \text{ mol}}{197.0 \text{ g}} \times \frac{6.02 \times 10^{23} \text{ atoms}}{1 \text{ mol}} = 3.06 \times 10^{24} \text{ atoms}$$

- How many moles of silver are in a sample containing 8.0×10^{25} atoms of silver?

$$8.0 \times 10^{25} \text{ atoms Ag} \times \frac{1 \text{ mol}}{6.02 \times 10^{23} \text{ atoms}} = 133 \text{ mol} = 130 \text{ mol} \leftarrow 2 \text{ sig figs}$$

- A typical banana contains 422 mg of potassium ~~ions~~ ^{atoms}. How many ~~ions~~ ^{atoms} is this?

$$422 \text{ mg K} \times \frac{0.001 \text{ g}}{1 \text{ mg}} \times \frac{1 \text{ mol}}{39.1 \text{ g}} \times \frac{6.02 \times 10^{23} \text{ atoms}}{1 \text{ mol}} = 6.50 \times 10^{21} \text{ atoms K}$$

